# Quantum Gyroscope 

Kiyohide NOMURA

Department of Physics, Kyushu University

## Gyroscope

Gyroscope: a device for measuring or maintaining orientation Example: Classical Gyroscope


## Classical Gyroscope

MOVIE: How to work classical gyroscope

## Classical Gyroscope

MOVIE: How to work classical gyroscope Based on the conservation of angular momentum

## Classical Gyroscope: airplane sensor

Sperry vertical gyro for Boeing 747 (airplane)


## Laser Gyroscope



Figure: ring laser gyro (from Encyclopedia Britannica)

Based on the relativity

## Laser Gyroscope



Figure: ring laser gyro (from Encyclopedia Britannica)

Based on the relativity Used in Boeing 777,787; Airbus A320 330/340,A380 etc.(airplane); Atlas I/II/III/V, H-IIA/B etc.(rocket)

## Laser Gyroscope: Sagnac effect



Figure: Light traveling opposite directions

Rotating circular ring

$$
\begin{equation*}
R: \text { radius, } \omega: \text { angular velocity, } c: \text { speed of light } \tag{1}
\end{equation*}
$$

A light source emits in both directions from one point on the ring

## Laser Gyroscope: Sagnac effect

- Light traveling in the same direction as the rotation It needs a catch up time $t_{1}$ as

$$
\begin{equation*}
t_{1}=\frac{2 \pi R+\Delta L}{c} \tag{2}
\end{equation*}
$$

$\Delta L$ : distance of rotating ring in the interval $t_{1}$

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Therefore

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- Light traveling in the opposite direction as the rotation

$$
\begin{equation*}
t_{2}=\frac{2 \pi R}{c+R \omega} \tag{5}
\end{equation*}
$$

## Laser Gyroscope: Sagnac effect

The time difference:

$$
\begin{equation*}
\Delta t=t_{1}-t_{2}=\frac{4 \pi R^{2} \omega}{c^{2}-R^{2} \omega^{2}} \tag{6}
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For $R \omega=v \ll c$

$$
\begin{equation*}
\Delta t \approx \frac{4 \pi R^{2} \omega}{c^{2}}=\frac{4 A \omega}{c^{2}} \tag{7}
\end{equation*}
$$

where $A=\pi R^{2}$ is the area of the ring.

## Laser Gyroscope

How to detect time difference?

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Interference of the light waves

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Interference of the light waves phase shift

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\Delta \phi=\frac{2 \pi c \Delta t}{\lambda} \tag{8}
\end{equation*}
$$

$\lambda$ : wavelength

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Figure:

## Laser Gyroscope: Sagnac effect



Figure:

For good interference, high quality light source is needed $\rightarrow$ Laser

## Quantum Gyroscope

Using the quantum interference

## Quantum Gyroscope

Using the quantum interference
only laboratory at present

- cold neutron (finite lifetime)
- laser cooled atomic gases (nK)
- superfluid He (2.17 K ( ${ }^{4} \mathrm{He}$ ); $2.49 \mathrm{~m} \mathrm{~K}\left({ }^{3} \mathrm{He}\right)$ )


## Short quantum physics; wave-particle duality

- wave behaves as a particle
- Energy $E$

$$
\begin{equation*}
E=h \nu=\frac{h c}{\lambda} \tag{9}
\end{equation*}
$$

( $h$ :Planck constant, $\nu$ : frequency, $\lambda$ : wave length)

- momentum $p$

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p=\frac{h}{\lambda} \tag{10}
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- particle behaves as a wave

$$
\begin{equation*}
\lambda=\frac{h}{p}=\frac{h}{m v} \tag{11}
\end{equation*}
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de Broglie theory

## Short thermodynamics; Superfluidity

Atoms in the ideal gas (statistical mechanics) MOVIE: Motion of gas atoms

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Atoms in the ideal gas (statistical mechanics) MOVIE: Motion of gas atoms
average velocity of atoms

$$
\begin{equation*}
\frac{3}{2} k_{B} T=\frac{1}{2} m\left\langle\boldsymbol{v}^{2}\right\rangle \tag{12}
\end{equation*}
$$

- $k_{\mathrm{B}}$ : Boltzmann constant
- $T$ : temperature


## Quantum phase transition

Lowering temperature, average velocity of atoms becomes slowing down.
$\rightarrow$
Wave length of atoms become larger
$\rightarrow$
Quantum interference becomes important at low temperatures MOVIE: Bose-Einstein Condensation

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Factors for quantum transitions:

- Temperature
- Density
- Mass of particles
- Fermion or Boson
- Dimensionality (2D or 3D)


## Superfluidity



Figure: heat capacity


Figure: zero viscosity

## Quantum Gyroscope: Superfluid Gyro



Figure:
R. W. Simmonds, A. Marchenkov, E. Hoskinson, J. C. Davis and R. E. Packard: Nature 412, $55-58$ (2001)

## Quantum Gyroscope: Superfluid Gyro

Interference pattern



Figure:

## Quantum Gyroscope: Superfluid Gyro

Weak Junction


Figure:
S. Narayana and Y. Sato: Phys. Rev. Lett. 106, 055302 (2011)

## Quantum Gyroscope: Superfluid Gyro

$$
\begin{equation*}
I_{c} \propto \cos \left(\pi \frac{2 \boldsymbol{\Omega} \cdot \boldsymbol{A}}{\kappa_{s}}\right) \tag{13}
\end{equation*}
$$

- $I_{c}$ : current
- $\Omega$ : Rotation vector
- A: Area vector
- $\kappa_{s}=h /\left(2 m_{s}\right)$ : quantum of circulation of ${ }^{3} \mathrm{He}$
- $h$ : Planck constant


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Comparison between laser and superfluid gyros

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m_{\mathrm{light}} \approx h \omega / c^{2} \tag{14}
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Superfluid gyro is expected highly sensitve!

Thank you for your attention.

